

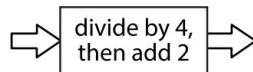
# 8th Grade Math Unit 5 Study Guide

## How to use:

- Solve a sample problem aligned to each lesson
- If you get stuck, look at the Lesson Summary for the lesson to help guide your thinking linked [here](#)
- Check your answer against the answer key linked [here](#)
- Practice explaining how you solved the problem and why your process makes sense!

## Lesson 1

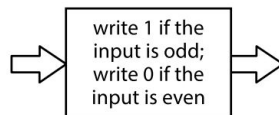
Given the rule:



Complete the table for the function rule for the following input values:

<b>input</b>	0	2	4	6	8	10
<b>output</b>						

Here is an input-output rule:



Complete the table for the input-output rule:

<b>input</b>	-3	-2	-1	0	1	2	3
<b>output</b>							

## Lesson 2

A group of students is timed while sprinting 100 meters. Each student's speed can be found by dividing 100 m by their time. Is each statement true or false? Explain your reasoning.

- Speed is a function of time.
- Time is a function of distance.
- Speed is a function of number of students racing.
- Time is a function of speed.

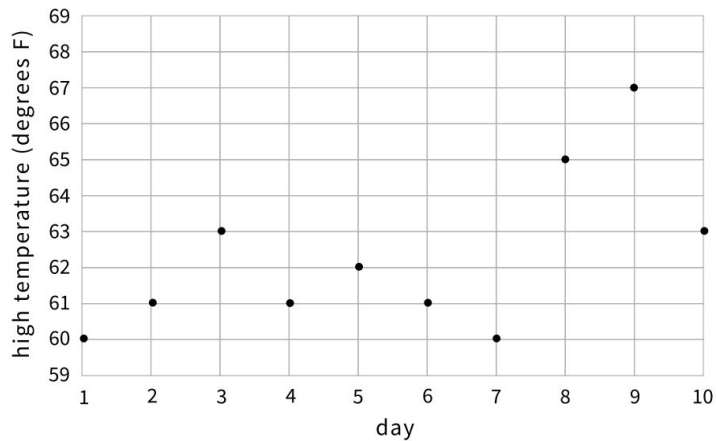
### Lesson 3

Brown rice costs \$2 per pound, and beans cost \$1.60 per pound. Lin has \$10 to spend on these items to make a large meal of beans and rice for a potluck dinner. Let  $b$  be the number of pounds of beans Lin buys and  $r$  be the number of pounds of rice she buys when she spends all her money on this meal.

- Write an equation relating the two variables.
- Rearrange the equation so  $b$  is the independent variable.
- Rearrange the equation so  $r$  is the independent variable.

### Lesson 4

The graph and the table show the high temperatures in a city over a 10-day period.

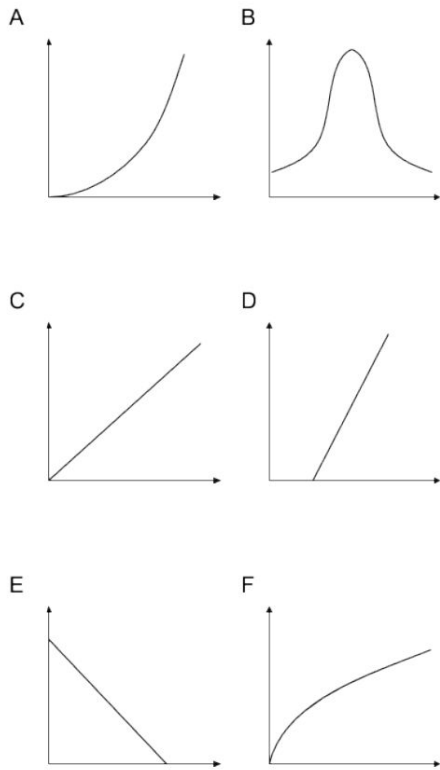


day	1	2	3	4	5	6	7	8	9	10
temperature (degrees F)	60	61	63	61	62	61	60	65	67	63

- What was the high temperature on Day 7?
- On which days was the high temperature 61 degrees?
- Is the high temperature a function of the day? Explain how you know.
- Is the day a function of the high temperature? Explain how you know.

## Lesson 5

Match each diagram to the function described, then label the axes appropriately

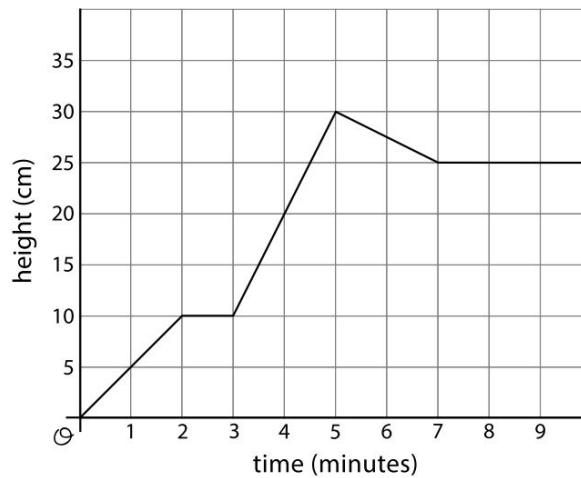


1. The function inputs the age of an oak tree  $a$  and outputs a prediction of the height of the tree  $h$ .
2. The function inputs the edge length  $e$  of a cube and outputs the volume  $v$ .
3. The function inputs the distance traveled  $d$  and predicts the amount of fuel left in the tank  $f$ .
4. The function inputs the height  $h$  of a triangle with base 12 and outputs the area  $a$ .
5. The function inputs the time of day  $t$  and predicts the temperature  $T$ .
6. The function inputs the time of day  $t$  and predicts the number of cars washed at a student car wash  $c$ .

## Lesson 6

Jada fills her aquarium with water.

The graph shows the height of the water, in cm, in the aquarium as a function of time in minutes. Invent a story of how Jada fills the aquarium that fits the graph.



## Lesson 7

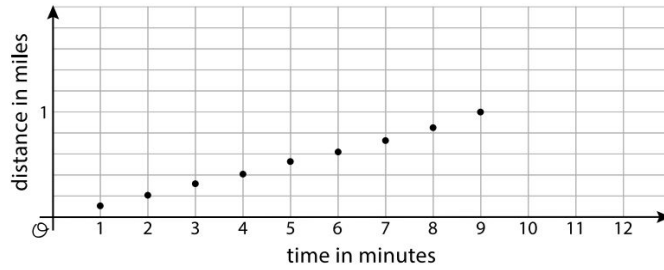
Elena and Lin are training for a race. Elena runs her mile a constant speed of 7.5 miles per hour.

Lin's times are recorded every minute:

<b>time (minutes)</b>	1	2	3	4	5	6	7	8	9
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<b>distance (miles)</b>	0.11	0.21	0.32	0.41	0.53	0.62	0.73	0.85	1
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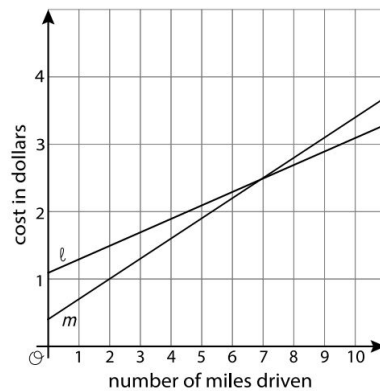
- Who finished their mile first?
- This is a graph of Lin's progress. Draw a graph to represent Elena's mile on the same axes.



- For these models, is distance a function of time? Is time a function of distance? Explain how you know.

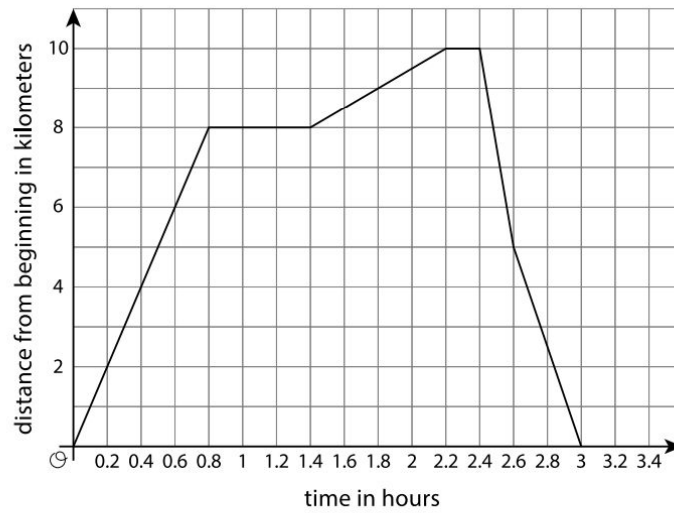
## Lesson 8

Two car services offer to pick you up and take you to your destination. Service A charges 40 cents to pick you up and 30 cents for each mile of your trip. Service B charges \$1.10 to pick you up and charges  $c$  cents for each mile of your trip.



- Match the services to the Lines  $\ell$  and  $m$ .
- For Service B, is the additional charge per mile greater or less than 30 cents per mile of the trip? Explain your reasoning.

## Lesson 10

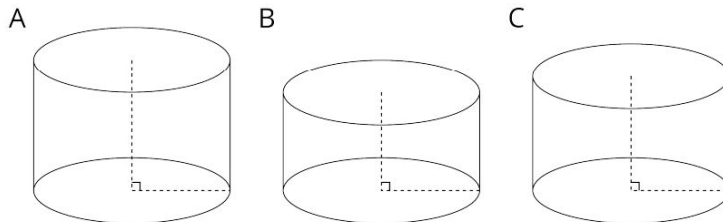


This graph shows a trip on a bike trail. The trail has markers every 0.5 km showing the distance from the beginning of the trail.

- When was the bike rider going the fastest?
- When was the bike rider going the slowest?
- During what times was the rider going away from the beginning of the trail?
- During what times was the rider going back towards the beginning of the trail?
- During what times did the rider stop?

## Lesson 11

Cylinder A, B, and C have the same radius but different heights. Put the cylinders in order of their volume from least to greatest.



## Lesson 12

- Sketch a cube and label its side length as 4 cm (this will be Cube A).
- Sketch a cube with sides that are twice as long as Cube A and label its side length (this will be Cube B).
- Find the volumes of Cube A and Cube B.

**Lesson 13**

Three cylinders have a height of 8 cm. Cylinder 1 has a radius of 1 cm. Cylinder 2 has a radius of 2 cm. Cylinder 3 has a radius of 3 cm. Find the volume of each cylinder.

**Lesson 14**

A cylinder has volume  $45\pi$  and radius 3. What is its height?

**Lesson 15**

A cylinder and cone have the same height and radius. The height of each is 5 cm, and the radius is 2 cm. Calculate the volume of the cylinder and the cone.

## Lesson 16

A cone has volume  $3\pi$ .

- If the cone's radius is 1, what is its height?
- If the cone's radius is 2, what is its height?
- If the cone's radius is 5, what is its height?
- If the cone's radius is  $\frac{1}{2}$ , what is its height?
- If the cone's radius is  $r$ , then what is the height?

## Lesson 17

A cylinder has a volume of  $48\pi \text{ cm}^3$  and height  $h$ . Complete this table for volume of cylinders with the same radius but different heights.

height (cm)	volume ( $\text{cm}^3$ )
$h$	$48\pi$
$2h$	
$5h$	
$\frac{h}{2}$	
$\frac{h}{5}$	

## Lesson 18

There are many cylinders with a height of 18 meters. Let  $r$  represent the radius in meters and  $V$  represent the volume in cubic meters.

- Write an equation that represents the volume  $V$  as a function of the radius  $r$ .
- Complete this table, giving three possible examples.

$r$	$V$
1	

- If the radius of a cylinder is doubled, does the volume double? Explain how you know.
- Is the graph of this function a line? Explain how you know.

## Lesson 19

A hemisphere fits snugly inside a cylinder with a radius of 6 cm. A cone fits snugly inside the same hemisphere.

- What is the volume of the cylinder?
- What is the volume of the cone?
- Estimate the volume of the hemisphere by calculating the average of the volumes of the cylinder and cone.

## Lesson 20

Match the description of each sphere to its correct volume.

- |                               |                                     |
|-------------------------------|-------------------------------------|
| A. Sphere A: radius of 4 cm   | 1. $288\pi \text{ cm}^3$            |
| B. Sphere B: diameter of 6 cm | 2. $\frac{256}{3}\pi \text{ cm}^3$  |
| C. Sphere C: radius of 8 cm   | 3. $36\pi \text{ cm}^3$             |
| D. Sphere D: radius of 6 cm   | 4. $\frac{2048}{3}\pi \text{ cm}^3$ |

## Lesson 21

Calculate the volume of the following shapes with the given information. For the first three questions, give each answer both in terms of  $\pi$  and by using 3.14 to approximate  $\pi$ . Make sure to include units.

- Sphere with a diameter of 6 inches
- Cylinder with a height of 6 inches and a diameter of 6 inches
- Cone with a height of 6 inches and a radius of 3 inches
- How are these three volumes related?